

This examination contains 5 problems on 2 pages. Please check that you have got the complete set. The numbers in parentheses with each problem signify the points to be earned for a perfect solution. The highest grade will be achieved with 60 points. So you have considerable freedom of choice.
Admissible aids: Pocket calculator, language dictionary (either electronic or in book form), lecture notes (hardcopy only, no electronic aids admitted except the pocket calculator.)

A useful formula:

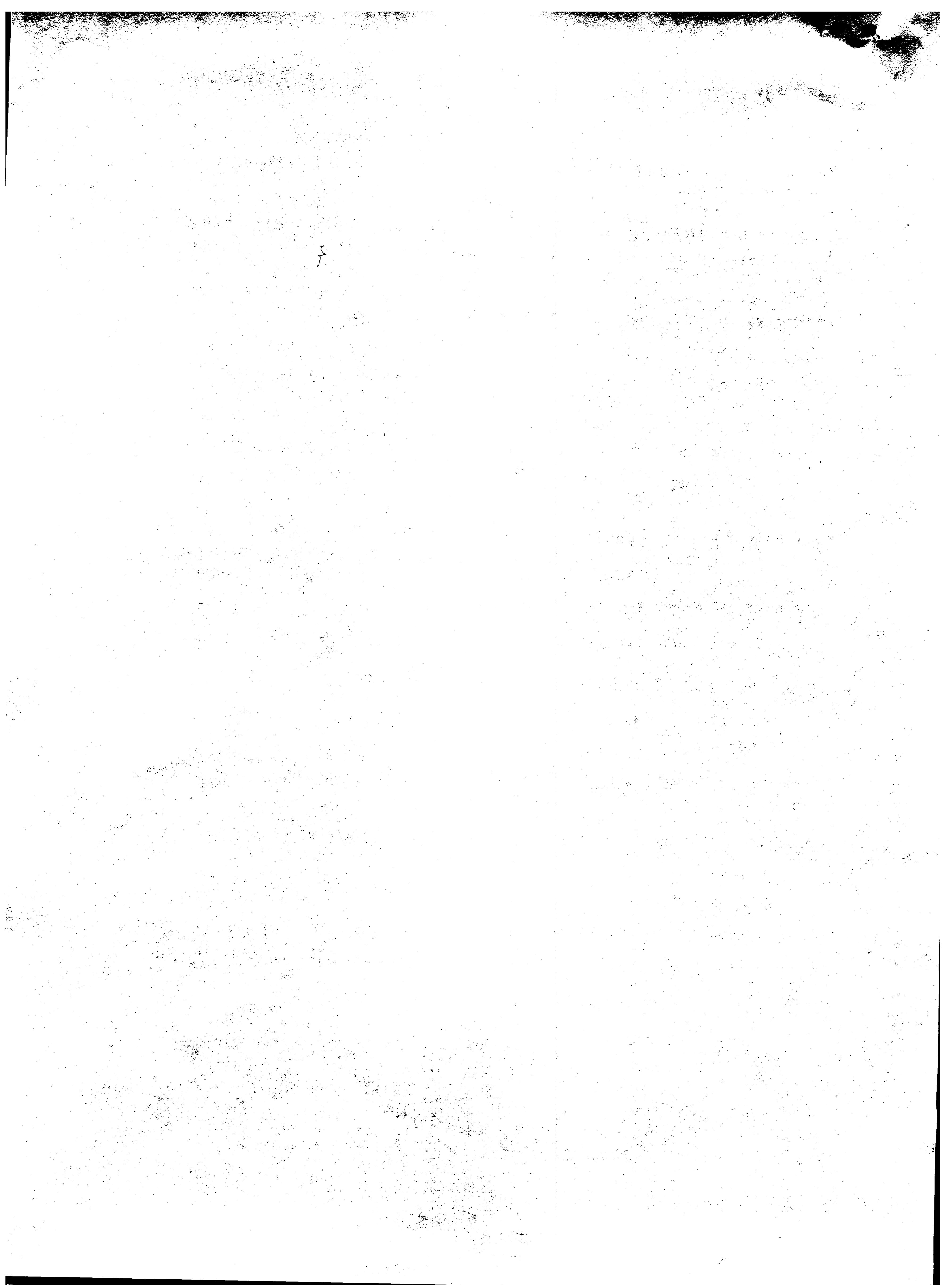
The certainty equivalent of a normally distributed payoff with expectation μ and variance σ^2 for a decision maker with constant absolute risk aversion ρ is $\mu - \rho\sigma^2/2$.

1	2	3	4	5	Σ	Grade
/16	/12	/15	/10	/30		

Problem #1: Consider a dual-product production process with the quantity q_j of output j constrained by: $q_j \leq F_j(K_j, L) = K_j L$; ($j=1,2$) where K_j denotes a product specific capital input and L a labor input common to both products. Let w denote the wage rate per unit of labor input L and p_j the user cost per unit of capital K_j . Assume $w=4$ and $p_1=p_2=1$.

- Determine the optimal factor inputs L^* , K_1^* , K_2^* as functions of the required output (q_1, q_2) . (8)
- Write down an explicit expression for the long-run cost function. (3)
- Write down an explicit expression for the short-run cost function on condition that $L=2$ has been fixed in advance. (2)
- Write down an explicit expression for the (long-run) cost function for partial program variation, given that $q_2=10$. (2)
- Indicate whether the production process has decreasing, constant or increasing returns to scale. (1)

Problem #2. A project generates cash flows of 14, 15 and 8 at the end of periods 1, 2 and 3, respectively. The acquisition cost, payable at the beginning of period 1 is 25. Determine the continuation present value at times 0, 1 and 2 and the economic incomes for periods 1 to 3 in two different ways. Assume a market interest rate of 5% p.a. (12)



Problem #3. Reconsider the project of problem #2. Assume the acquisition cost is depreciated using the straight line method. Determine:

- the accounting incomes from the project for periods 1 to 3. (3)
- the residual incomes from the project in these two periods. (6)
- Check that Preinreich's theorem holds at times 0 and 1. (6)

Problem #4. Assume the normal capacity of a maintenance unit is 1600 maintenance hrs per month. Normal cost at this capacity is € 32 000, € 20 000 of which are fixed. In November last year 1200 hrs of maintenance work were done. The actual cost amounted to € 30 000. Calculate

- the amount of maintenance cost absorbed (2)
- the flexible cost budget $C(x)$ as a function of actual volume x , (3)
- the efficiency variance (3)
- and the (unabsorbed) cost of idle capacity (2)

Problem #5. A firm wants its manager to maximize its accounting profit. Profit before management compensation is $G(a) = 3a + \varepsilon$ where a denotes the manager's effort level and ε a normally distributed random variable with zero mean and variance $\sigma^2 = 10$. The manager's personal cost of effort is $C(a) = a^2/2$, his CARA is $\rho = 0.2$, and his reservation wage $U^{-1}(U) = 1$.

- Calculate the optimal effort level assuming effort is observable (first-best effort level) and the resulting profit after management compensation (4)
- State the manager's decision problem when he faces a linear contract offering a share s of $G(a)$ and a fixed salary F . Determine the optimal effort level and the optimal objective function value for the manager (8)
- State the principal's problem in formal terms, concerning the optimal linear contract he should offer to a manager who behaves according to part c. (10)
- Calculate the optimal share of the profit $G(a)$ and the optimal fixed salary in a linear incentive scheme. (4)
- Calculate the Agency Costs (4)

