

End-Term Test
Production Management & Operations Research
February 7, 2003

Last name: **First name:** **Matriculation number:**

Assignment # 1 (10 points)

„In order sequencing, for a given set of orders, the minimization of the average order processing time and the minimization of the total waiting time of all orders are equivalent goals.“

- a) Give a definition of the average order processing time!
- b) Give a general proof of the above statement!

Do not forget to define all the symbols properly you have to introduce!

Assignment #2 (20 points)

Five product types are to be manufactured in a three-stage production process. The operation times for the corresponding production orders (A, B, C, D, E) differ for these three stages, as can be seen from the table below.

| production stage production order | (1) | (2) | (3) |
|--------------------------------------|-----|-----|-----|
| A | 3 | 4 | 6 |
| B | 7 | 4 | 2 |
| C | 6 | 4 | 8 |
| D | 6 | 1 | 4 |
| E | 4 | 1 | 5 |

The sequence of stages, which the orders have to pass through, is identical for all orders. Overtaking of orders is not permitted.

- a) Apply Johnson's Algorithm to this three-stage problem! How many solutions gives Johnson's Algorithm in this case?
- b) For each solution, plot the corresponding GANTT-chart!
- c) Determine the cycle times of the solutions! Which is the best solution? Is the best solution an optimal one?

Assignment # 3 (20 points)

The following table lists those work elements (operations), which have to be carried out on a production line on which car stereos of a specific type are produced. The list also includes information on the operation times of the work elements and the relevant precedence relationships.

| work element i | operation time t_i | direct predecessor(s) |
|-------------------|-------------------------|--------------------------|
| 1 | 30 | - |
| 2 | 52 | - |
| 3 | 45 | 2 |
| 4 | 23 | 1, 3 |
| 5 | 15 | 1, 3 |
| 6 | 45 | 2 |
| 7 | 45 | 5, 6 |
| 8 | 45 | 4, 7 |

The desired average output rate is 40 stereos per hour.

- a) What is the maximal cycle time, which cannot be exceeded if 40 stereos are to be produced per hour?
- b) What is the theoretical minimum number of work stations for the desired output rate?
- c) For the precedence relationships given in the above table, plot the corresponding precedence diagram?
- d) Assign the work elements according to the method of Helgeson and Bernie!
- e) How many work stations are necessary? Also determine the total idle time and the capacity utilization of this solution!
- f) Is the solution an optimal one?